

Fig. 3. Ball-and-stick drawings of the coordination polyhedra for (a) $\mathrm{Ga}(1)$, (b) $\mathrm{Ga}(2)$, and (c) Mg . The site symmetries for these atoms are $4 \mathrm{~mm}, \mathrm{~m}$ and mm , respectively. In all cases, the $c$ axis is vertical. Numerals indicate the type of Ga atoms. The central atom is stippled.

Just as gallium possesses a unique structure among the elements, it appears that $\mathrm{Ga}_{5} \mathrm{Mg}_{2}$ may also have a unique structure. A search of standard references such
as Pearson's (1967) book reveals no $A_{5} B_{2}$ compounds isotypic with $\mathrm{Ga}_{5} \mathrm{Mg}_{2}$. Nor does Mg , in fact, form an $A_{5} \mathrm{Mg}_{2}$ phase with any of the other Group IIIA elements.

We thank Drs C.K.Johnson and A. Zalkin for furnishing copies of the several IBM-7094 programs used in the calculations, and V.Silveira for powder photography.

## References

Cromer, D. T. (1965). Acta Cryst. 18, 17.
Furnas, T. C. (1957). Single Crystal Orienter Instruction Manual. Milwaukee: General Electric Company.
Haucke, W. (1938). Naturwissenscahften, 26, 577.
Hume-Rothery, W. \& Raynor, G. V. (1938). J. Inst. Metals, 63, 201.
International Tables for X-ray Crystallography (1952). Vol. I. Birmingham: Kynoch Press.

International Tables for X-ray Crystallography (1962). Vol. III. Birmingham: Kynoch Press.

Pearson, W. B. (1967). A Handbook of Lattice Spacings and Structures of Metals and Alloys. Vol.2. Oxford: Pergamon Press.
Sharma, B. D. \& Donohue, J. (1962). Z. Kristallogr. 117, 293.

Smith, G. S., Mucker, K. F., Johnson, Q. \& Wood, D. H. (1969). Acta Cryst. B 25, 549.

Teatum, E., Gschneidner, K. \& Waber, J. (1959). Los Alamos Scientific Laboratory Report, No. LA 2345.

Acta Cryst. (1969). B25, 557

# The Crystal Structure of $\mathbf{Z r}_{4} \mathbf{C o}_{4} \mathbf{G e}_{7}$ (V-Phase) 

By Wolfgang Jeitschko<br>Department of Metallurgy, University of Illinois, Urbana, Illinois, U.S.A.

(Received 25 March 1968)
The crystal structure of the V-phase $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ has been determined by single-crystal X-ray diffraction analysis. The structure is of a new type with four formula units in a tetragonal unit cell of space group I4/mmm ( $D_{4 h}^{17}$ ), having the dimensions $a=13.228 \pm 0.004, c=5.229 \pm 0.003 \AA$ and $c / a=0.3952 \pm 0.0002$. The structure was refined by the least-squares method, giving a final $R$ value of 0.092 for the 392 independent structure factors observed. It may be characterized as intermediate between the tetrahedrally close packed structures ( $\sigma$-phase related structures, Laves phases) and the structures of the $\mathrm{CuAl}_{2}$-type family.

## Introduction

In their study of the ternary system titanium-nickelsilicon, Westbrook, DiCerbo \& Peat (1958) reported the occurrence of a ternary phase of the composition $\mathrm{Ti}_{4} \mathrm{Ni}_{4} \mathrm{Si}_{7}$ to which they ascribed the name ' V -phase'. Subsequently Jordan (1963) found thirteen isotypic compounds in which the large titanium atoms were replaced by zirconium, niobium or tantalum, the smaller transition metal component nickel by cobalt and iron, and germanium could substitute silicon. The phases were
reported to be nearly homogeneous at the composition 4:4:7, with the possible exemption of two phases, where the exact composition has not been determined. While investigating similar ternary systems (including hafnium as the larger transition metal component) Markiv, Gladyševskij \& Fedoruk (1966), Markiv, Gladyševskij, Kripjakevič \& Fedoruk (1966) and Markiv (1966) independently discovered a number of isotypic phases at the approximate composition $1: 1: 2$, having a body-centered tetragonal unit cell. This unit cell could be used to index the powder patterns of the V-
phases and it appears therefore that the compounds found by the Ukraine-Russian authors are isotypic with the V-phases. This conclusion is also supported by the similar lists of representatives given by Jordan (1963) and Markiv (1966) (Table 1.) The present investigation was undertaken to establish the crystal structure of these phases.

Table 1. V-phases found by Jordan (1963), +, and Markiv (1966),*


## Experimental

Specimens and powder patterns of the V-phases were made available to the author through the kindness of Professor P.A. Beck and Mr A. G.Jordan of this laboratory. From the pronounced graininess of the powder photograph of $\mathrm{Zr}_{4} \mathrm{CO}_{4} \mathrm{Ge}_{7}$ it could be concluded that the sample had large grains and therefore was favorable for the isolation of single crystals. The sample which had been prepared from the components of purity greater than $99.9 \mathrm{wt} . \%$, and annealed at $1100^{\circ} \mathrm{C}$ for four days, was found upon metallographic examination to contain $\sim 3 \%$ of a second phase. The presence of the second phase was probably caused by a $0.5 \%$ weight loss of mainly germanium (the most volatile component) during the arc melting, thus shifting the overall composition of the sample slightly towards a higher transition metal content. This explains also the somewhat higher experimental density of $8.13 \pm 0.08 \mathrm{g.cm}-3$ versus the value of $8.05 \mathrm{~g}_{\mathrm{cm}}{ }^{-3}$ deduced from the structure determination.
Several single crystals, isolated from the crushed sample, were examined with a Buerger precession camera (Mo $K \alpha$ radiation) and a Weissenberg goniometer (Cr $K \alpha$ and Mo $K \alpha$ radiation). The body-centered tetragonal unit cell as reported by Markiv (1966) ( $a=13 \cdot 20, c=5 \cdot 23 \AA$ ) was confirmed and the following lattice constants were obtained by the least-squares refinement of data taken with a 114.6 mm diameter Debye-Scherrer camera and $\mathrm{Cr} K \alpha$ radiation ( $\lambda_{K \alpha_{1}}=$ 2.28962 $\AA$ ):

$$
\begin{aligned}
a & =13 \cdot 228 \pm 0.004, & & c
\end{aligned}=5 \cdot 229 \pm 0.003 \AA \AA .
$$

To facilitate the identification of V-phases, the observed and calculated intensities (using the positional parameters from the refined structure and a computer program by Jeitschko \& Parthé, 1966) for a DebyeScherrer diagram are listed in Table 2.

For the structure determination and refinement, intensity data were collected with a Weissenberg camera, with Mo $K \alpha$ radiation and the multiple film technique (five films interleaved with Cu foils). Intensities were escimated visually with the aid of an intensity strip, which was logarithmically scaled in steps of $10 \%$. The reciprocal lattice planes ( $h k 0$ ), ( $h k 1$ ), ( $h k 2$ ), ( $h h l$ ) and ( $h, h-1, l$ ) were evaluated. The two single crystals selected for these photographs were both of elongated prismatic shape with rectangular cross-sections and

Table 2. Calculated and observed intensities of the $V$-phase $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$
Debye-Scherrer camera, $\operatorname{Cr} K \alpha$ radiation.

| h | k |  | $d_{c}(\stackrel{\circ}{A})$ | $\mathrm{I}_{\mathrm{c}}$ | $I_{0}$ | $\mathrm{hk} \ell$ | $d_{c}(\stackrel{\circ}{A})$ | $\mathrm{I}_{\mathrm{c}}$ | $I_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 9.3536 | 2 | - | 840 | 1.4789 | 4 | Vw |
| 2 | 0 | 0 | 6.6140 | 1 | - | 910 | 1.4608 | 0 | - |
| 1 | 0 | 1 | 4.8628 | 0 | - | 503 | 1.4555 | 14 |  |
| 2 | 2 | 0 | 4.6768 | 0 | - | 433 | 1.4555 | 14 | S |
| 3 | 1 | 0 | 4.1831 | 0 | - | 732 | 1.4468 | 9 | w |
| 2 | 1 | 1 | 3.9179 | 0 | - | 523 | 1.4215 | 1 | - |
| 3 | 0 | 1 | 3.3709 | 0 | - | 901 | 1.4149 | 2 | vvw |
| 4 | 0 | 1 | 3.3070 | 0 | - | 802 | 1.3975 | 0 | - |
| 3 | 3 | 0 | 3.1179 | 1 | - | 930 | 1.3944 | 2 | VVW |
| 3 | 2 | 1 | 3.0033 | 1 | - | 921 | 1.3836 | 0 |  |
| 4 | 2 | 0 | 2.9579 | 0 | - | 761 | 1.3836 | 51 | vw |
| 4 | 1 | 1 | 2.7346 | 1 | - | 822 | 1.3673 | 5 | vw |
| 0 | 0 | 2 | 2.6145 | 14 | w | 613 | 1.3601 | 1 | - |
| 5 | 1 | 0 | 2.5942 | 4 | vw | 851 | 1.3543 | 2 | vVw |
| 1 | 1 | 2 | 2.5180 | 0 | - | 662 | 1.3390 | 2 | vVw |
| 2 | 0 | 2 | 2.4314 | 0 | - | 770 | 1.3362 | 2 | vVw |
| 4 | 3 | 1 | 2.3607 | 51 |  | 543 | 1.3322 | 3 | VVW |
| 5 | 0 | 1 | 2.3607 | 49 | vvs | $7 \quad 52$ | 1.3255 | 2 | vVw |
| 4 | 4 | 0 | 2.3384 | 17 | w | 860 | 1.3228 | 0 |  |
| 2 | 2 | 2 | 2.2821 | 6 | vw | 1000 | 1.3228 | 23 | vvw |
| 5 | 3 | 0 | 2. 2686 | 1 | - | 004 | 1.3072 | 16 |  |
| 5 | 2 | 1 | 2. 2233 | 4 |  | 633 | 1.3060 | 1 |  |
| 3 | 1 | 2 | 2. 2171 | 46 | vs | 941 | 1.3009 | 0 | - |
| 6 | 0 | 0 | 2.2047 | 23 | m | 1020 | 1.2971 | 1 | - |
| 6 | 2 | 0 | 2.0915 | 2 | vvw | 114 | 1.2947 | 0 | - |
| 4 | 0 | 2 | 2.0510 | 8 | vw | 842 | 1.2873 | 9 |  |
| 6 | 1 | 1 | 2.0079 | 2 |  | 950 | 1.2848 |  | w |
| 3 | 3 | 2 | 2.0034 | 11 | w | 204 | 1. 2824 |  |  |
| 4 | 2 | 2 | 1.9589 | 13 | w | 703 | 1. 281.2 |  | vo |
| 5 | 4 | 1 | 1.9214 | 5 | vw | 1011 | 1. 2764 |  |  |
| 7 | 1 | 0 | 1.8707 | 0 |  | 912 | 1.2752 | 7 | w |
| 5 | 5 | 0 | 1.8707 | 7 | w | 224 | 1.2590 | 0 | - |
| 6 | 3 | 1 | 1.8451 | 1 | - | 723 | 1.2578 | 1 | - |
| 5 | 1 | 2 | 1.8415 | 0 | - | 3114 | 1.2477 | 0 | - |
| 6 | 4 | 0 | 1.8344 | 3 | vw | 1031 | 1.231 .4 | 8 |  |
| 7 | 0 | 1 | 1.7772 | 7 | W | 932 | 1. 2303 | 2 | w |
| 4 | 4 | 2 | 1.7430 | 0 | - | 1040 | 1.2282 | 32 | $s$ |
| 7 | 3 | 0 | 1.7369 | 5 | vw | 404 | 1.2157 | 0 | - |
| 1 | 0 | 3 | 1.7281 | 0 | - | 653 | 1.2147 | 9 | w |
| 7 | 2 | 1 | 1.7163 | 1 | - | 871 | 1:2106 | 6 | vw |
| 5 | 3 | 2 | 1.7135 | 0 | - | $3 \quad 34$ | 1.2056 | 0 | - |
| 6 | 0 | 2 | 1.6854 | 0 | - | 1110 | 1.1976 | 0 | - |
| 2 | 1 | 3 | 1.6719 | 0 | - | 424 | 1.1957 | 0 |  |
| 8 | 0 | 0 | 1.6535 | 3 | vw | 743 | 1.1947 | 1 |  |
| 6 | 2 | 2 | 1. 6332 | 4 | VW | 813 | 1.1947 | 5 ) | Vw |
| 3 | 0 | 3 | 1. 6209 | 0 | - | 961 | 1.1908 | 0 | - |
| 6 | 5 | 1 | 1.6113 | 7 | w | 772 | 1.1898 | 27 | $s$ |
| 8 | 2 | 0 | 1. 6041 | 1 | - | 862 | 1.1803 | 11 |  |
| 3 | 2 | 3 | 1. 5744 | 0 | - | 1002 | 1.1803 | 37 |  |
| 8 | 1 | 1 | 1. 5655 | 3 | Vw | 1101 | 1.1720 | 5 | vw |
| 7 | 4 | 1 | 1. 5655 | 0 | vw | 880 | 1.1692 | 0 | - |
| 6 | 6 | 0 | 1.5589 | 1 | - | 514 | 1. 1674 | 4 | vvw |
| 7 | 5 | 0 | 1.5377 | 0 | - | 1022 | 1.1620 | 4 | vVw |
| 4 | 1 | 3 | 1.5316 | 0 | - | 970 | 1. 1602 | 1 | - |
| 5 | 5 | 2 | 1.5214 | 4 |  | 1130 | 1.1602 | 1 | - |
| 7 | 1 | 2 | 1.521 .4 | 2 | w | 833 | 1.1575 | 0 | - |
| 6 | 4 | 2 | 1.5016 | 0 | - | 10.51 | 1.1540 | 66 |  |
| 8 | 3 | 1 | 1. 4845 | 0 | - | 1121 | 1.1540 | 0 |  |

both were mounted with the needle axis perpendicular to the primary X-ray beam. The one, rotating around the [001] axis, had the dimensions $0.03 \times 0.05 \times 0.20 \mathrm{~mm}$ the other, with dimensions $0.03 \times 0.03 \times 0.15 \mathrm{~mm}$, was rotating around the [110] direction. Absorption corrections were made, assuming cylindrical shapes for the crystals (International Tables for X-ray Crystallography, 1959). After applying the proper Lorentz-polarization corrections, the structure factors were brought to a common scale by deriving average scale factors using those data present on corresponding films.

## Derivation of the approximate structure

From the value of the experimental density mentioned above, the number of formula units per cell was calculated to be $4 \cdot 04 \simeq 4$. The only systematic extinctions observed were those of the body-centered unit cell, and, since the values of $|F(h k l)|$ and $|F(\bar{h} k l)|$ were equal within the limits of error, the structure is of high Laue symmetry, thus reducing the choice to five possible space groups with the general diffraction symbol $I 4 / * * *$ (Donnay \& Kennard, 1964).

It was noticed that the reciprocal lattice layers with $\Delta l= \pm 4$ were equal except for the normal decline with higher $l$-values. The quantitative evaluation of the two Weissenberg photographs $(h, h, l)$ and $(h, h-1, l)$ showed that this relation held up to $l=12$, which was the limit of the Mo $K \alpha$-sphere. Thus the structure is layered with atoms arranged in planes which are $\Delta z=\frac{1}{4}$ apart. This made it possible to compute threedimensional Patterson functions with the data ( $h k 0$ ), ( $h k 1$ ) and ( $h k 2$ ) only. In order to do this, unitary structure factors were calculated by dividing the observed structure factors by the average atomic scattering coefficient and the average temperature factor, which was obtained from a Wilson plot (Wilson, 1942). The unitary structure factors of the reciprocal planes $l>2$ were then set equal to the corresponding planes $l \leq 2$. The evaluation of the three-dimensional sharpened Patterson function calculated with these data, using a computer program by Sly, Shoemaker \& van den Hende (1962), turned out to be difficult, since even on


Fig. 1. Unitary structure factors in the reciprocal lattice plane ( $h k 0$ ) of $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$, showing pseudo-octagonal symmetry.
the basis of the Patterson function no unambigous decision could be made among the five possible space groups. Since, however, the $z$-projection symmetry for the five space groups is the same, it was attempted to gain as much information as possible from the ( $h k 0$ ) data first.

A number of considerations were helpful for the tentative placement of atoms in the $z$ axis projection:
(a) The unitary structure factor $U_{10100}$ has a value very close to unity. Thus one can draw a sublattice which offers 21 possible locations for the placement of the $3 \frac{3}{4}$ atoms within the asymmetric unit.
(b) Because of the pseudo-octagonality of the ( $h k 0$ ) reciprocal lattice net (Fig. 1) the arrangement of atoms around the [100] and [110] axes has to be similar in the $z$-projection.
(c) The length of the $z$ axis makes a placement of two zirconium atoms above each other extremely unlikely.
(d) Additional information was obtained from an electron-density projection computed with about 15 structure factors, for which the signs had been determined with the aid of Harker-Kasper inequalities (Harker \& Kasper, 1948).

The combined results of these considerations provided several positions which were likely to be occupied. These positions were then tried out systematically - by assuming distinct $z$ parameters - as starting positions for the interpretation of the three-dimensional Patterson function with the superposition method (a detailed description of this method is given by Shoemaker, Barieau, Donohue \& Lu, 1953). After several trials a self-consistent set of atomic positions was obtained. The distribution of the three kinds of atoms was then concluded from the interatomic distances, the weights of the Patterson peaks and from the atomic arrangements in related compounds. An intensity calculation with this trial structure gave an $R$ value (defined throughout the paper as $R=\Sigma\left|F_{o}-F_{c}\right| / \Sigma F_{o}$ ) of 0.18 for the observed structure factors, indicating that the structure was essentially correct.

## Structure refinement

The structure was refined on the University of Illinois IBM 7094 computer with a full-matrix least-squares program (Gantzel, Sparks \& Trueblood, 1961) and the function minimized was $\Sigma w^{2}(\Delta F)^{2}$ with $w=1 / F_{\text {obs }}$. Although the structure may be described with all five space groups of $I 4 * * *$, the space group with the highest symmetry: $I 4 / m m m-D_{4 h}^{17}$ was chosen for the refinement. This is the most probable space group, since the description of the structure in space groups $I \overline{4} 2 m$, $I \overline{4} \mathrm{~m} 2$ and $I 4 \mathrm{~mm}$ would allow, besides an increase in the number of $x$ and $y$ parameters, three or six additional $z$ parameters, which are not required because of the layered nature of the structure, as mentioned above. The fifth possible space group, $I 422$, was not ruled out initially, since it requires only one additional parameter: the 16 cobalt atoms of position $16(\mathrm{k})$ in $I 4 / \mathrm{mmm}$
need to be placed in $8(j)$ of $I 422$ with $x_{1} \simeq 0.15$ and $x_{2} \simeq 0 \cdot 35$. This would allow for a staggering of the cobalt atoms rather than a straight alignment along the $z$ axis as required by space group $I 4 / \mathrm{mmm}$. However the least-squares refinement in $I 422$ revealed a strong intcraction of the two Co parameters and therefore the refinement was completed in the centrosymmetric space group. This decision was justified later by the Fourier synthesis along the $z$ axis, which gave no indication of a staggering of the Co atoms.

The values of the atomic scattering factors were taken from International Tables for X-ray Crystallography (1962) and were corrected for the real part of the anomalous dispersion (Dauben \& Templeton, 1955). Using the ( $h k 0$ ), ( $h k 1$ ), and ( $h k 2$ ) data a total of 14 parameters was refined: the six positional $x$ parameters, the isotropic temperature parameters for the atomic positions and one general scale factor. The $z$ parameter of $\mathrm{Ge}(4)$ was refined separately from the ( $h h l$ ) and the ( $h, h-1, l$ ) data. These are most sensitive to the $z$ parameters and were also considered to be more reliable, since they were collected with a smaller crystal whose shape resembled more closely that of a cylinder, for which the absorption correction was made. The final value for this parameter was $z=$ $0 \cdot 252 \pm 0 \cdot 002$. Since this value deviates only insignificantly from $\frac{1}{4}$ it was preferred to fix it with the idealized value $z=0 \cdot 250$ and to increase the limits of error correspondingly. Six additional least-squares cycles were then run using all the observed data. The refinement was considered to be complete when the shifts of all parameters in the last three cycles were within the standard deviations computed from the inverse matrix. Table 3 lists the final parameters. The residual value for the 392 observed structure factors (Table 4) is $R=0.092$.

Since the atomic scattering powers in $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ are not very different, it was considered worthwhile to perform a test for possible disorder. Using a leastsquares program originally written by Busing, Martin \& Levy (1962) and later revised by Stucky, two leastsquares cycles were run whereby the occupancy factors only were refined. The resulting values for these factors varied between 0.96 (for the Co position) and 1.01 ( $\mathrm{Ge}(4)$ position) with standard deviations of the order of 0.02 . Thus it was concluded that the initial atomic distribution is essentially correct. As with most intermetallic compounds, however, a disorder in the range of some atomic per cent must be regarded as possible.

Table 4. Observed and calculated structure factors of $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$

|  | F |  |  | $F_{0}$ | ${ }_{\text {c }}$ |  |  | ${ }^{\text {c }}$ |  | ${ }_{5}$ |  |  | $F_{\text {o }}$ |  |  | $\mathrm{F}_{0}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\ell=0$ |  |  | 18 | 8150 | 39 | 25 | <46 | -18 | $\begin{array}{\|l\|} \hline 17 \\ 19 \\ 18 \end{array}$ | $\begin{aligned} & 16<47 \\ & 16<47 \end{aligned}$ | $\begin{aligned} & -11 \\ & -14 \end{aligned}$ |  | $\begin{aligned} & 7<48 \\ & 8146 \end{aligned}$ |  | $0 \quad 0^{2}=870^{4} 1059$ |  |  |
|  |  |  | 20 | 69 | 68 | 27 | <45 | -38 |  |  |  |  |  |  |  |  |  |
| 0 |  | 35 | 22 | 45 | 40 | 43 | 395 | 486 |  | $\begin{array}{rrr} 9 & 16 & <47 \\ 8 & 17 & 84 \end{array}$ |  | 10 | 61 | $-161$ |  |  |  |
| 2 | 0 - | 38 | 24 | 53 | 61 | 63 | 9 | 94 |  |  |  | 12 | 8178 | -164 |  | $2<51$ | 11 |
| 4 | <41 | 19 | 26 | <45 | -20 |  | 28 | -25 | 047662 |  |  | 14 |  | -69 | 14444 |  |  |
| 6 | O 5336 | 120 | 9 |  | -73 | 10 | 206 | 220 |  | O $\begin{array}{r}1476 \\ 0\end{array}$ | ${ }_{-37}^{628}$ |  |  |  |  |  |  |
| 10 | 297 | 293 | 13 | 35 | -12 | 14 | 129 | 108 |  | ${ }^{\circ} \mathrm{O} 34$ | 353 | 20 | ${ }_{8} 15$ | -58 | 355 |  | $325$ |
| 12 | $0<67$ | 42 | 15 | 9106 | 90 | 16 | <40 | 20 | 6 | ${ }^{\circ}$ | 32 | 22 | 46 | $\rightarrow$ |  | 194 | 195 |
| 14 | 0524 | 592 | 17 | 61 | -57 | 18 | 180 | 173 |  |  | 16 | 24 | 62 | -51 | 8 |  | 17 |
| 16 | <69 |  | 19 | 41 | 11 | 20 | 45 | 34 | 10 | 163 -14 |  | 26 | 85 | -85 |  | <6B | -55 |
| 18 | $0<69$ | -58 | 21 | $9<42$ | 26 | 22 | 85 | -84 | 12 |  |  | 28 | 56 | -57 | 10 | 10482 | 519 |
| 20 | 0338 | 365 | 23 |  | -78 | 24 | 3119 | 120 | 140 | - 220 | 177 | 9 | 94 | -94 |  | $11<7$ | 56 |
| 22 | 97 | 102 | 25 |  | 22 | 26 | <46 | 19 | $\begin{aligned} & 16 \\ & 18 \\ & 20 \end{aligned}$ |  | 132 | 11 | 85 | -70 |  | $12<83$ | 55 |
| 24 | 78 | 68 | 1010 | 0648 | 676 | 28 | 46 |  |  | 0 | -18 | 13 | 9224 | 219 |  | 1389 | -88 |
| 26 | $0<64$ | 45 |  | $0{ }^{63}$ | 65 | 54 | 177 | 209 |  | 0 99 | 94 | 15 | <42 | -12 |  | 234 | 225 |
| 28 | 0114 | 122 |  | $0{ }^{71}$ | 65 | 74 | 78 | 81 | 220 |  | 53 | 17 | <43 | -19 |  | 1515 | 48 |
| 34 | 106 | 117 | 1610 | 0180 | 155 |  | <39 |  | 24 | ${ }^{0} 153$ | 157 | 19 | 82 | -84 |  | $16<87$ | 28 |
| 1 | 1 - | -67 |  | 0179 | 164 | 11 | 228 | 237 |  |  | -76 | 21 | 04 | -87 |  | <86 |  |
| 3 | 68 | 50 |  | 0120 | 106 | 13 | 119 | 119 | $\begin{array}{ll} 26 \\ 28 & 0 \\ 30 & 0 \end{array}$ | 0 0 0 0 | 15 | 23 | 56 | 50 |  | $18<85$ | 20 |
| 5 | 160 | 158 | 2210 | $0<46$ |  | 15 | 196 | -191 |  | 0116 | 117 | 25 | 54 | $-1$ |  | $19<83$ | 5 |
| 7 | $1<21$ |  |  | 0240 | 215 | 17 | 166 | 157 | $\begin{array}{ll}1 \\ 3 & 1 \\ 3 & 1\end{array}$ | 119 | -19 | 27 | 60 | 59 |  | 145 |  |
| 9 | 31 | 34 |  | <43 | 16 | 19 | <42 | 24 |  | 1406 -509 |  | 29 | <45 | -23 |  |  |  |
| 11 | <26 | ${ }^{-3}$ | 1111 | B0 | 70 | 21 | <43 | 15 | $\begin{array}{ll}5 & 1 \\ 7 & 1 \\ 9 & 1\end{array}$ |  | -63 | 1010 | 10236 | 231 |  |  |  |
| 13 | 130 | $-122$ | 1311 | 46 | 47 | 23 | <45 | 43 |  |  | $\begin{array}{llll}1 & 139 & 144 \\ 1 & 253 & -250\end{array}$ |  | 1210 | $10<50$ | 18 |  | $0<55$ | 0 |
| 15 | 146 | 133 |  | $1<39$ |  | 25 | <45 | 18 |  |  |  |  | 1410 | 10196 | 193 |  | $1<55$ | 0 |
| 17 | 78 | 81 | 1711 | 145 | S | 27 | <46 | 35 | 11 | -2 | -287 | 1610 | 1065 | -67 |  | <56 | 5 |
| 19 | 80 | -76 |  | 147 | 45 | 6 | 234 | 256 |  |  | -46 | 18 | $10<47$ |  |  | 285 |  |
| 21 | <40 | 13 |  | c44 | 36 | 8 | 1 | -147 | ll 17 |  |  | 2010 | 10220 | 8 |  | 4129 |  |
| 23 | <44 | 10 | 2311 | 192 | $-77$ | 10 | 338 | -351 |  |  |  | 2210 | 1048 | -49 | 6 | 5174 | -155 |
| 25 | $1<46$ | 17 |  | 146 | 60 | 18 | 109 | -105 | 191 | $\begin{array}{llll}1 & 154 & -1 \\ 1 & 103\end{array}$ | -91 | 2410 | $10 \quad 57$ | 45 |  | 6126 | 34 |
| 27 | $1<47$ | -13 |  | 2 <66 | 71 | 14 | 202 | -199 |  | $\begin{array}{lllllll}21 & 1 & <53 & 35\end{array}$ |  | 2610 | 1055 | 48 | 8 | 105 | 98 |
| 29 | $1<44$ | 26 | 1412 | 256 | -56 | 16 | 129 | 125 | ${ }^{23} 12$ | 1116 | -120 | 2810 | $10<47$ | 26 |  | <78 | 37 |
| 2 | $2<28$ | 8 |  | $2<40$ | -21 | 18 | <41 | -16 |  | 50-50 |  | 2111 | 11210 | 102 |  | 94 | 5 |
| 4 | $2<20$ | 8 |  | $2<41$ |  | 20 | . 75 | 173 | ${ }^{27}$ | $1<50$ |  | 1311 | 11195 | 184 |  | 0 <80 | 52 |
| 6 | 2172 | -171 | 2012 | $2<43$ | 29 | 22 |  | -87 |  | 1 $<48$ -27 <br> 2 203 -238 <br>  254  <br>  277 -324 |  | 1511 | 1175 |  |  | $1<82$ | 10 |
| 8 | 2136 | -127 |  | $2<43$ | 10 | 24 | - | $-76$ |  |  |  | 1711 | 11124 | -58 |  | $12<85$ | -20 |
| 10 | 186 | 155 |  | $2<42$ | -20 | 26 | <46 | -42 |  |  |  | 1911 | 1155 | -58 |  | 13106 |  |
| 12 | 37 | 30 | 1313 | - | -108 | 28 | <43 | -29 | $\begin{array}{ll} 4 & 2 \\ 6 & 2 \\ 8 & 2 \end{array}$ | $277-200$ |  | 2111 | 1196 | -92 |  | $14<86$ | -19 |
| 14 | 2136 | -121 | 1513 | $3<40$ | 21 | 76 | 192 | 213 |  | $2208-211$ |  | 2311 | $11<55$ | -39 |  |  |  |
| 16 | $2<36$ |  |  | 3127 | 129 |  | <32 |  | $\begin{array}{ll} 10 & 2 \\ 12 & 2 \end{array}$ | 105-111 |  | 2511 | $11<55$ | -28 | 0343 |  |  |
| 18 | 33 | -28 | 1913 | 3108 | -93 | 11 | <35 |  |  | 279 -72 |  | $2711<53$ |  |  |  |  |  |  |
| 20 | <42 | -10 | 21.13 | $3<43$ | -11 | 13 | 135 | 126 | 12 | 2154 | -136 | 1212 | $12<45$ | -22 |  | $1<65$ | 18 |
| 22 | <43 |  |  | $3<42$ | 17 | 15 | 53 | -56 | 16 |  |  |  |  |  | $2 \begin{array}{lllll}2 & 2114 & -116\end{array}$ |  |  |
| 24 | <44 | -2 |  | 4259 | 259 | 17 | <42 | - 22 |  | $\begin{aligned} & 2125 \\ & 2<50 \end{aligned}$ | -132 |  | 1412178 | -60 -50 | 4 4 273 -30 <br> 5 5 150 141 |  |  |
| 26 | <43 | -8 | 1614 | 1438 | -39 | 19 | -44 | -37 | 18 | $\begin{array}{ll} 2<50 & -19 \\ 2 & 52 \\ \hline \end{array}$ |  | $\begin{array}{llll}18 & 12 & 65 & -50 \\ 20 & 12 & 54 & -48\end{array}$ |  |  |  |  |  |  |
| 28 3 | ${ }^{47}$ | -50 |  |  | 185 | $2{ }_{2}^{21}$ | ${ }_{54}^{68}$ | 56 | $\begin{aligned} & 22 \\ & 24 \\ & 24 \end{aligned}$ | $2{ }_{2}{ }^{56}$ |  | 2212 | 12 $12 \begin{aligned} & 54 \\ & 12\end{aligned}$ | ${ }_{-32}^{-48}$ | $\begin{array}{ccccc}5 & 5 & 150 & 141 \\ 6 & 6 & 135 & -127\end{array}$ |  |  |
| 5 | 121 | 108 |  | 4 <42 | 28 | 25 | 44 | -49 | 26 | <51 | -25 | ${ }_{24}^{24} 12<52{ }^{2}$ |  |  | 284 |  |  |
| 7 | 346 | 371 |  | $4<41$ | 5 | 27 | 45 | 13 | 28 | 66 | -64 | 2612 | $12<49$ | 20 | 8 | 8 88 |  |
| 9 | 199 | -196 |  | 5209 | 179 | 8 | 44 | 148 |  | 335 | 423 | 2812 | 1282 | 69 |  | ${ }^{283}$ | 57 |
| 11 |  |  |  |  |  | 10 | <31 | 13 |  | 50 | -49 | 1313 | $13<48$ |  |  | 85 | 44 |
| 13 | 144 | 144 | 19 | 43 | 19 | 12 | 160 | 154 | 7 | 245 | -283 | 1513 | $13<53$ | 15 |  | 85 | 69 |
| 15 | $<37$ | -12 |  | 554 | 62 | 14 | 260 | 274 |  | 107 | -111 | 1713 | 13103 | 90 |  | 12 <85 | 16 |
| 17 | 95 | 90 |  | <41 | 22 | 16 | <41 | 27 | 11 | 153 | 174 | 1913 | $13{ }^{88}$ | 83 |  | 13 <86 |  |
| 19 | <41 | 28 | 1616 |  | 33 | 18 | 44 |  | 13 | 251 | -246 |  | $13{ }^{54}$ | 41 |  | $14{ }^{\text {< } 87}$ | 16 |
| 21 | 84 | 88 | 1816 | $6<43$ | -10 | 20 | 47 | 54 | 15 | 154 | 148 | 2313 | 13136 | 18 |  |  | 81 |
| 23 | 112 | -104 | 20 | 1 | -5 | 22 | <46 |  | 17 | $3121-119$ |  | $2713<5249$ |  |  | $0^{2}=67$ |  |  |
| 25 | 346 | 51 | 2216 | $6<41$ | 17 | 24 | 87 | 71 | 1921 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 27 | 129 | 130 | 1717 | 780 | 82 | 26 | 56 | 49 |  | 3 102 -101 <br> 3 $<99$ -26 |  | $1614<5314$ |  |  |  |  |  |
| 29 | 68 | -68 |  | $17<43$ | 31 | 28 |  |  | 23 |  |  | 4 $\begin{array}{llllr}2 & 2 & <68 \\ 3 & 2 & <69 & -1 \\ 5\end{array}$ |  |  |  |  |  |  |
| 4 | 471 | 512 |  | 7105 | 102 | 98 | 57 | 56 |  | <55 | 42 |  |  |  | 1814 | 1475 | 74 |
| 6 | 4217 | -220 | 23 | <43 | -47 | 11 | 40 | -35 |  | <55 | -25 |  | 14 <54 |  | 4 | 3196 | 85 |
| 8 | 257 | -286 | 1818 | $8<62$ | 2 | 13 | 104 | 104 | 29 | 56 | -69 | 221 | 14 <5s |  |  |  | -84 |
| 10 | 530 | 618 |  | $8{ }^{172}$ | -11 | 15 |  | 13 |  | 23 | -73 | 2414 | $14{ }^{61}$ | 66 |  |  |  |
| 12 | -32 | -16 | 2218 | $8<42$ | -40 | 17 | 40 | -37 |  | 32 | -25 | 2614 | 14 99 | 88 |  | 94 | 94 |
| 14 | 121 | -95 |  | $9<57$ |  | 19 | <46 | -8 |  | 216 | -254 | 1515 | 15123 | 18 | 8 | 70 | 71 |
| 16 | 56 | 5 |  | 947 | -49 | 21 | <49 | 5 | 10 | 18 | 109 | 1715 | 15 54 | 52 |  | $8<72$ |  |
| 18 | 98 | 101 | 2319 | - $<37$ | -22 | ${ }^{23}$ |  | 57 | 12 | 72 | -77 | 1915 | $15<53$ | 8 |  |  |  |
| 20 | <41 | 31 | 2020 | 20170 | 164 | 25 | 54 | -44 | 14 | - | 12 | 2115 | $15<54$ | 35 |  |  |  |  |
| 22 | 44 | $-54$ |  | <37 | 23 | 27 | <44 | - | 16 | 168 | -171 | $\begin{array}{lllll}25 & 15 & <52 & \\ 16 & 16 & 91 & -97\end{array}$ |  |  |  |  |  |  |
| 24 | 147 | 151 |  |  |  | 12 | 146 | - 14 | 18 | $53-66$ |  |  |  |  |  |  |  |
| 28 | <42 | ${ }_{-54}^{-12}$ |  |  |  |  |  |  | 22 | 128 <br> $<56$ <br> 5113 <br> -14 |  | 1816 | 16124 |  |  |  |  |
| 28 5 | ${ }_{434}^{44}$ | -54 |  |  | 16 | 14 | $\begin{aligned} & <39 \\ & <41 \end{aligned}$ | -4 | 22 <br>  <br> 26 <br> 26 |  |  | 1816 | $16<55$ | -196 |  | $2<74$ |  |
| 7 | 43 | 39 | 50 | 563 | -68 | 18 |  | 46 |  | <55 | 13 |  | 16 <5s | -27 |  |  | 30 |
| 9 | 64 | 151 | 70 | - 372 | 362 | 20 | 53 | -63 | 28 | <52 | -31 | 2416 | 1675 | -64 | 4 | 4180 | ${ }^{173}$ |
| 11 | 158 | 140 |  | 217 | -204 | 22 | 45 | -13 |  | 127 | 289 |  | 17180 | 177 |  |  | $\begin{array}{r}154 \\ 73 \\ \hline\end{array}$ |
| 13 | <37 | 11 | 11 | 0167 | -148 | 24 | 45 | -7 |  | 127 | -139 |  |  | -66 |  | 780. | 3 |
| 15 | 203 | 192 | 13 | 0131 | 117 | 26 | 46 | -7 | 9 | <31 | 17 | 2117 | $17<54$ | -32 |  |  |  |
| 17 | 74 | 68 | 15 | 181 | -164 | 1110 |  | - | 11 | 33 | 26 | 2317 | $17<51$ | 13 |  |  | 31 |
| 19 | 112 | 104 | 17 | <41 | 15 |  | - $<42$ | 20 | 13 | 100 | -108 |  |  | -54 |  |  | -31 293 |
| 21 | <43 | ${ }_{-7} 3$ | 19 | 191 | 85 | 1510 |  | -250 | 15 | <45 |  |  |  | -54 |  |  | 293 |
| 23 | <45 |  | 21 | 100 | ${ }^{85}$ |  | ${ }^{6} 63$ | -68 | 19 |  | 29 |  |  | -77 |  |  |  |
| 27 27 |  | $\begin{array}{r}14 \\ 34 \\ \hline\end{array}$ | 25 |  | -27 |  | $0<48$ | -16 | 21 | 53 | -34 |  | $18<48$ | -36 |  | $0<3$ |  |
|  | 222 | 210 | 27 | <45 | 19 |  | $0<48$ | $-3$ | 23 | 52 | -49 | 1919 | $19<55$ | -12 | 2 | $1 \times 73$ |  |
|  | 56 | 55 | 29 | <42 | -31 |  |  | -37 | 25 | 64 | 57 |  | 1952 | -48 |  |  | 124 |
| 10 | <34 | 21 | 2 | 13 |  | 1211 | $1<40$ | 14 | 29 |  | -11 |  |  | -87 |  |  |  |
| 12 | <37 | -36 | 4 | 54 | -47 | 1411 | 1<42 | -2 | 29 |  |  |  | $20<53$ 20 | 17 -2 |  | 4 <br> 5 <br> $<75$ <br> 75 |  |
| 14 | 136 | ${ }_{-71}^{210}$ | ${ }_{8}^{6}$ | 1136 1 1 173 | 124 | 1611 |  | 126 |  | 229 | -240 |  | 20-49 | 88 |  |  |  |
| 16 | 130 | ${ }_{-126}^{-71}$ | 10 | $\begin{array}{ll}1 \\ 1 \\ 1 & 173 \\ 177\end{array}$ | ${ }_{-172}^{171}$ | 1811 |  | -17 | 10 | ${ }_{6}^{6} 163$ | 180 | 21 | $21 \quad 55$ | 83 63 | 8 | $7<75$ | 49 |
| 20 | 168 | 164 | 12 | 66 | -64 | 2211 | 17 | -69 | 12 | 171 | -183 |  | 21 |  |  | $8<75$ | 17 |
| 22 | <42 | 24 | 14 | 147 | 123 | 2411 | 161 | 64 | 14 | 88 | -85 |  | 22 | 22 |  |  |  |
| 24 | <44 | -29 | 16 | <40 | 18 |  |  | 28 | 16 | <48 | -19 |  |  |  |  |  |  |
| 26 | <45 | 6 | 18 | <42 | 15 | 1512 |  | - 103 | 18 | 102 |  |  |  |  |  |  |  |
| 7 | 286 | 6 6 | 20 | 44 | -32 | 1712 | 253 | -50 | 20 | $6<52$ | - -21 |  | $\begin{array}{ll} 0<40 \\ 1 & <40 \end{array}$ | 1 | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | $\begin{aligned} & 1<76 \\ & 2<76 \end{aligned}$ | -6 <br> -54 |
| 9 | ${ }^{68}$ | 66 | 22 | <42 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 116 $<36$ | -111 | 24 | <44 | -29 |  |  | -52 | 26 |  | - 29 | 4 | ${ }^{2}<293$ | 381 | 4 | $4<75$ | 17 |
| 13 | ${ }_{145}$ | -18 | 28 | 49 | -60 | 1413 | 146 | 145 | 28 | 59 | -56 | 5 | 4186 | -169 |  | $5<75$ | 62 |
| 17 | 247 | 246 | 3 | 17 | 2 |  |  | 37 |  | 431 | 504 | 6 | 5222 |  | 6 | $6<74$ | -64 |
| 19 | 139 | -120 | 5 | 162 | -158 | 1813 |  | 58 |  | 236 | -247 |  |  |  |  |  |  |
| 21 | 106 | 83 | 7 | 2110 | 108 | 2013 | 3 <48 | 28 | 11 | 7223 |  |  | 7155 868 | ${ }^{126}$ |  | ${ }_{9}^{8} \mathrm{Cl}_{71}$ |  |
| 23 | 69 | 15 |  |  |  |  |  |  |  |  |  | 10 | $8<69$ 9 | ${ }_{-121}^{48}$ |  | - 9 ¢ 272 | -30 |
| 27 |  | 24 | 15 |  | -92 | 19 | ${ }^{4} 46$ | -54 | 19 | 7104 | -102 | 121 | $11<73$ | 12 |  |  |  |
| 10 | 75 | -71 | 17 |  | -49 |  |  | 103 | 21 |  | 149 |  | $12<76$ | -24 |  | - 0198 |  |
| 12 | 62 | -48 | 19 | <42 | 21 |  |  | -54 | 23 |  | -94 | 141 | 13129 | 1 |  | 10 | 153 |
| 1 | 8 |  |  |  | -24 | 1815 | 572 | -65 | 25 | 55 | -61 | 151 | 14 <81 |  |  |  |  |
| 16 | 65 | -58 | 23 |  | 23 |  |  | -95 | 27 | 7107 | 108 |  |  |  |  |  |  |

Table 3. Atomic parameters of $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ and their standard deviations

|  | Position | $x$ | $\sigma(x) \times 10^{4}$ | $y$ | $\sigma(y) \times 10^{4}$ | $z$ | $\sigma(z)$ | $B\left[\AA^{2}\right]$ | $\sigma(B)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $8 \mathrm{Zr}(1)$ | $8 h$ | 0.1390 | 3 | 0.1390 | 3 | 0 | - | 0.52 | 0.03 |
| $8 \mathrm{Zr}(2)$ | $8 j$ | 0.6962 | 2 | $\frac{1}{2}$ | - | 0 | - | 0.52 | 0.03 |
| 16 Co | $16 k$ | 0.1482 | 2 | 0.6482 | 2 | $\frac{1}{4}$ | - | 0.54 | 0.03 |
| $8 \mathrm{Ge}(1)$ | $8 h$ | 0.2934 | 3 | 0.2934 | 3 | 0 | - | 0.49 | 0.04 |
| $8 \mathrm{Ge}(2)$ | $8 i$ | 0.2918 | 2 | 0 | - | 0 | - | 0.42 | 0.04 |
| $8 \mathrm{Ge}(3)$ | $8 j$ | 0.9069 | 2 | - | 0 | - | 0.53 | 0.04 |  |
| $4 \mathrm{Ge}(4)$ | $4 e$ | 0 | - | 0 | - | 0.250 | 0.004 | 0.47 | 0.04 |

## Discussion

The V-phase structure (Fig.2) may be described as intermediate between two structure families: the tetrahedrally close packed structures and the $\mathrm{CuAl}_{2}$-type family. The tetrahedrally close packed structures are characterized by the predominance of fairly regular coordination polyhedra of coordination numbers (C.N.) 12, 14, 15 and 16 (Frank \& Kasper, 1958, 1959). Shoemaker \& Shoemaker (1968a) have proposed the name 'tetrahedrally close packed structures' for these phases, since they have slightly distorted tetrahedral voids only. They have typically metallic character, i.e. their occurrence and varying compositions are governed by valence electron rules (Greenfield \& Beck, 1956; Das \& Beck, 1960; Bardos \& Beck, 1966; Laves \& Witte, 1936; Klee \& Witte 1954; Nevitt, 1963; Wernick, 1967). This group of compounds may be divided into two subgroups. The one, commonly called the $\sigma$-phase related structures (for references see Shoemaker \& Shoemaker, 1968a, b) is formed by metals of not more than $15 \%$ difference in atomic radii (C.N. 12). The structures of the other subgroup, the Laves phases ( $\mathrm{MgNi}_{2}-, \mathrm{MgCu}_{2^{-}}$and $\mathrm{MgZn}_{2}$-type, for references see Nevitt, 1963) are formed by elements differing about 10 to $60 \%$ in atomic radii. These
structures are distinguished from the $\sigma$-phase related structures in so far as they have C.N. 12 and C.N. 16 polyhedra only. The lack of intermediate coordination polyhedra is probably responsible for the occurrence of the Laves phases in ternary systems along the pseudobinary sections $A(B, C)_{2}$ only, in contrast to the $\sigma$-phase related structures where the C.N. 14 and C.N. 15 sites can accomodate both small and large atoms (Shoe-maker \& Shoemaker, 1965).

The $\mathrm{CuAl}_{2}$ family comprises a number of structures ( $\mathrm{CuAl}_{2}-, \mathrm{U}_{3} \mathrm{Si}_{2}-, \mathrm{C}_{5} \mathrm{~B}_{3}$-type sructures) which may be described as stacking variants of the tessellation net 32.4.3.4, formed by the larger atoms only (Aronsson, 1961). The structure types $\mathrm{W}_{5} \mathrm{Si}_{3}, \mathrm{Mn}_{5} \mathrm{Si}_{3}$ and $\mathrm{Ti}_{5} \mathrm{Ga}_{4}$ (for references see Schubert, 1964) with a transition metal/meta metal ratio similar to that of the V-phase may be regarded, like the V-phase structure, as intermediate between the tetrahedrally close packed structures and the structures of the $\mathrm{CuAl}_{2}$ family (Aronsson, 1961). The structural relationships among these various silicide structure types have been discussed by Parthé, Lux \& Nowotny (1955) and Nowotny (1963).

Like most of the tetrahedrally close packed structures and the structures of the $\mathrm{CuAl}_{2}$ family, the V phase is a layered structure. It has two identical main layers at $z=0$ and $\frac{1}{2}$, translated, relative to each othe


Fig. 2. Structure of the $V$-phase $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ as compared to the structures of $\mathrm{Hf}_{2} \mathrm{Ge}$ and $\mathrm{FeGe}_{2}$ (both crystallizing in the $\mathrm{CuAl}_{2-}$ type) and $\mathrm{TiFe}_{2}$ ( $\mathrm{MgZn}_{2}$-type). The outlined building elements in the $\mathrm{CuAl}_{2}$ and $\mathrm{MgZn}_{2}$-type structures are very similar to those present in $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$. In the drawing of the $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ structure the atoms at $z=\frac{1}{2}$ are connected with thick lines, atoms at $z=0$ with thin lines and non connected atoms are superimposed with $z=\frac{1}{4}$ and $\frac{3}{4}$.
by half the base diagonal. These layers are formed by the Zr atoms and the Ge atoms (1), (2) and (3) which are in contact with each other, thus forming a tessellation of pentagons, squares and triangles (Fig. 2). The Co and $\mathrm{Ge}(4)$ atoms are situated at $z=\frac{1}{4}$ and $\frac{3}{4}$ and have no close neighbors within their layers. The structure exhibits a high degree of close packing.* However it should not be considered as a purely tetrahedrally close packed structure since some of the tetrahedra have edges differing by more than $40 \%$ in length; furthermore it does not contain Frank-Kasper polyhedra only. It is interesting to note that the tetrahedrally close packed structures and the structures of the $\mathrm{CuAl}_{2}$ family occur most frequently in the binary systems of the components forming a V-phase. The structural relationship of the V-phase to these structure types can be demonstrated by comparison of the coordination polyhedra.

As can be seen from Fig. 3 the environments of the Zr atoms (1) and (2) are the same, if one disregards some minor differences in the interatomic distances (Table 5). This coordination polyhedron may be derived from the Frank-Kasper polyhedron C.N. 15 by replacing each of two atoms from the 'belt' by a pair of atoms at the same level, whereby the C.N. is increased to 17 . A similar arrangement is also found around the $\mathrm{Hf}^{\mathrm{I}}$ atom in $\mathrm{Hf}_{3}^{\mathrm{I}} \mathrm{Hf}_{2}^{\mathrm{II}} \mathrm{Sn}_{4}\left(\mathrm{Ti}_{5} \mathrm{Ga}_{4}\right.$-type, Rossteutscher \& Schubert, 1965) where the places of Zr are taken by $\mathrm{Hf}^{\mathrm{I}}$, those of Co by HfII and those of Ge by Sn. The coordination polyhedra for the Co and $\mathrm{Ge}(2)$ atoms are distorted icosahedra, which are present in all tetrahedrally close packed structures. The environment of $\mathrm{Ge}(1)$ is the same as that of $\mathrm{Ge}(2)$ except for the replacement of two neighboring Ge atoms by a Zr atom. This C.N. 11 polyhedron is also found for the Ge atoms in $\mathrm{Zr}_{5} \mathrm{Ge}_{3}\left(\mathrm{Mn}_{5} \mathrm{Si}_{3}\right.$-type, Parthé \& Norton, 1958), where the places of both transition metals Zr and Co are occupied by Zr . The coordination around $\mathrm{Ge}(3)$ is the Frank-Kasper polyhedron C.N. 14. However, the distance of $2.46 \AA$ to one of the crystallographically equivalent Ge atoms is very close to the covalent bonding distance of $2.45 \AA$ in elemental germanium (diamond-type). Thus the Ge(3) atoms may be considered as forming pairs. The Ge atoms in $\mathrm{Th}_{3} \mathrm{Ge}_{2}$ ( $\mathrm{U}_{3} \mathrm{Si}_{2}$-type, Tharp, Searcy \& Nowotny, 1958) and $\mathrm{FeGe}_{2}\left(\mathrm{CuAl}_{2}\right.$-type, Krén \& Szabó, 1964) have similar environments with short $\mathrm{Ge}-\mathrm{Ge}$ distances of $2 \cdot 4_{8}$ and 2.62 respectively. The $\mathrm{Ge}(4)$ atoms are situated in a tetragonal antiprism of Zr atoms with two Ge atoms above and below the square faces. This C.N. 10 polyhedron is also found for the Ge atoms in $\mathrm{Hf}_{2} \mathrm{Ge}$ ( $\mathrm{CuAl}_{2}$-type, Nowotny, Benesovsky \& Schob, 1960) and the Si atoms of the fourfold positions in $\mathrm{Nb}_{5} \mathrm{Si}_{3}$

[^0]and $\mathrm{Ta}_{5} \mathrm{Si}_{3}\left(\mathrm{~W}_{5} \mathrm{Si}_{3}\right.$-type, Parthé, Nowotny \& Schmid, 1955).

In Table 5 the interatomic distances in $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ are compared with the sum of the atomic radii for C.N. 12. There is a strong interaction of the transition metals with germanium (all distances $\mathrm{Zr}-\mathrm{Ge}$ and Co-Ge are shorter than the corresponding sums of the C.N. 12 radii). The distances $\mathrm{Zr}-\mathrm{Zr}, \mathrm{Zr}-\mathrm{Co}$ and $\mathrm{Co}-\mathrm{Co}$ are all longer. The only short $\mathrm{Ge}-\mathrm{Ge}$ distances are found for $\mathrm{Ge}(4)$, forming chains and $\mathrm{Ge}(3)$ forming pairs as already mentioned above.

The author wishes to thank Professor P.A. Beck for suggesting this work, as well as for many stimulating discussions. Thanks are also due to Mr A. G. Jordan who was kind enough to furnish specimens and powder photographs of the V-phases. This work was supported by a grant from the Army Research Office, Durham.

## References

Aronsson, B. (1961). Ark. Kemi, 16, 379.
Bardos, D. I. \& Beck, P. A. (1966). Trans. Amer. Inst. Min. (Metall.) Engrs. 236, 64.
Busing, W. R., Martin, K. O. \& Levy, H. A. (1962). ORFLS, A Fortran Crystallographic Least-Squares Program. Report ORNL-TM-305, Oak Ridge National Laboratory, Oak Ridge Tennessee.
Das, B. N. \& Beck, P. A. (1960). Trans. Amer. Inst. Min. (Metall.) Engrs. 218, 733.


Fig.3. Coordination polyhedra in $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$. Co atoms are represented by black spheres, Zr and Ge atoms by large and small white spheres respectively. The environment of $\mathrm{Zr}(1)$ and $\mathrm{Zr}(2)$ is shown in $c$ and $f ; a, b$ and $g$ are the coordination polyhedra of $\mathrm{Ge}(4), \mathrm{Ge}(2)$ and $\mathrm{Ge}(1)$ respectively; $d$ shows the distorted icosahedron around the Co atoms and $e$ is the coordination polyhedron around a pair of $\mathrm{Ge}(3)$ atoms. A cube with the cube edge $a=c / 2$ as seen from the same viewpoint is drawn in $h$.

Dauben, C. H. \& Templeton, D. H. (1955). Acta Cryst. 8, 841.

Donnay, J. D. H. \& Kennard, O. (1964). Acta Cryst. 17, 1337.

Frank, F. C. \& Kasper, J. S. (1958). Acta Cryst. 11, 184.
Frank, F. C. \& Kasper, J. S. (1959). Acta Cryst. 12, 483.
Gantzel, P. K., Sparks, R. A. \& Trueblood, K. N. (1961). Program UCLALS 1, University of California.
Greenfield, P. \& Beck, P. A. (1956). J. Metals, 8, 265.
Harker, D. \& Kasper, J. S. (1948). Acta Cryst. 1, 70.
International Tables for X-ray Crystallography (1959). Vol. II, Table 5.3.5B. Birmingham: Kynoch Press.
International Tables for X-ray Crystallography (1962). Vol. III, Table 3.3.1A (for Co and Ge ) and Table 3.3.1B (for Zr ). Birmingham: Kynoch Press.
Jeitschko, W. \& Parthé, E. (1966). A Fortran IV Program for the Intensity Calculation of Powder Patterns. Report of the Laboratory for Research on the Structure of Matter, Univ. of Pennsylvania, Philadelphia, Pennsylvania.

Jordan, A. G. (1963). M. S. Thesis, University of Illinois, Department of Metallurgy.
Klee, H. \& Witte, H. (1954). Z. Phys. Chem. 202, 352.
Krén, E. \& Szabó, P. (1964). Phys. Letters, 11, 215.
Laves, F. \& Witte, H. (1936). Metallwirtschaft, 15, 840.
Markiv, V. Ja. (1966). Acta Cryst. 21, A 84.
Markiv, V. Ja., Gladyševskij, E. I. \& Fedoruk, T. I. (1966). Izv. Akad. Nauk SSSR, Metally, 1966, 179.

Markiv, V. Ja., Gladyševskij, E. I., Kripjakevič, P. I. \& Fedoruk, T. I. (1966). Izv. Akad. Nauk SSSR, Neorgan. Mat. 2, 1317.
Nevitt, M. V. (1963). In Electronic Structure and Alloy Chemistry of the Transition Elements. P. A. Beck, ed., New York: John Wiley.
Nowotny, H. (1963). In Electronic Structure and Alloy Chemistry of the Transition Elements. P. A. BECK, ed., New York: Wiley.
Nowotny, H., Benesovsky, F. \& Schob, O. (1960). Mh. Chem. 91, 270.

Table 5. Interatomic distances $D$ and coordination numbers C.N. in the structure of $\mathrm{Zr}_{4} \mathrm{Co}_{4} \mathrm{Ge}_{7}$ For comparison the sum of the atomic radii ( $C N 12$ ) is listed too. All distances shorter than $3 \cdot 8 \AA$ are given.

|  |  | D [ $\AA$ ] | $r_{A}+r_{B}[\AA]$ | $\Delta[\AA]$ |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \operatorname{Zr}(1) \\ & \mathrm{C} . \mathrm{N} .17 \end{aligned}$ | $4 \mathrm{Zr}(2)$ | $3 \cdot 285 \pm 3$ | $3 \cdot 20$ | $+0.09$ |
|  | $2 \mathrm{Zr}(1)$ | $3 \cdot 677 \pm 9$ | $3 \cdot 20$ | $+0.48$ |
|  | 4 Co | $3 \cdot 106 \pm 6$ | $2 \cdot 86$ | $+0.25$ |
|  | $2 \mathrm{Ge}(2)$ | $2 \cdot 732 \pm 3$ | 2.97 | -0.24 |
|  | $1 \mathrm{Ge}(1)$ | $2.888 \pm 9$ | 2.97 | -0.08 |
|  | $2 \mathrm{Ge}(1)$ | $2 \cdot 904 \pm 5$ | 2.97 | $-0.07$ |
|  | $2 \mathrm{Ge}(4)$ | $2 \cdot 910 \pm 12$ | $2 \cdot 97$ | $-0.06$ |
| $\begin{aligned} & \mathrm{Zr}(2) \\ & \mathrm{C} . \mathrm{N} .17 \end{aligned}$ | $4 \mathrm{Zr}(1)$ | $3 \cdot 285 \pm 3$ | $3 \cdot 20$ | +0.09 |
|  | $2 \mathrm{Zr}(2)$ | $3 \cdot 670 \pm 5$ | $3 \cdot 20$ | $+0.47$ |
|  | 4 Co | $3 \cdot 129 \pm 3$ | $2 \cdot 86$ | $+0.27$ |
|  | $2 \mathrm{Ge}(1)$ | $2 \cdot 736 \pm 6$ | $2 \cdot 97$ | -0.23 |
|  | $1 \mathrm{Ge}(3)$ | $2.787 \pm 5$ | $2 \cdot 97$ | -0.18 |
|  | $2 \mathrm{Ge}(2)$ | $2 \cdot 904 \pm 3$ | $2 \cdot 97$ | $-0.07$ |
|  | $2 \mathrm{Ge}(4)$ | $2 \cdot 906 \pm 11$ | 2.97 | -0.06 |
| $\begin{aligned} & \text { Co } \\ & \text { C.N. } 12 \end{aligned}$ | $2 \mathrm{Zr}(1)$ | $3 \cdot 106 \pm 6$ | 2.86 | $+0.25$ |
|  | $2 \mathrm{Zr}(2)$ | $3 \cdot 129 \pm 3$ | $2 \cdot 86$ | $+0.27$ |
|  | 2 Co | $2 \cdot 615 \pm 2$ | $2 \cdot 52$ | $+0 \cdot 10$ |
|  | $2 \mathrm{Ge}(1)$ | $2 \cdot 448 \pm 5$ | $2 \cdot 63$ | $-0 \cdot 18$ |
|  | ${ }_{2} \mathrm{Ge}(3)$ | $2 \cdot 466 \pm 4$ | $2 \cdot 63$ | -0.16 |
|  | $2 \mathrm{Ge}(2)$ | $2 \cdot 486 \pm 3$ | $2 \cdot 63$ | -0.14 |
| $\begin{aligned} & \mathrm{Ge}(1) \\ & \text { C.N. } 11 \end{aligned}$ | $2 \mathrm{Zr}(2)$ | $2 \cdot 736 \pm 6$ | $2 \cdot 97$ | $-0.23$ |
|  | ${ }_{1} \mathrm{Zr}(1)$ | $2.888 \pm 9$ | 2.97 | $-0.08$ |
|  | $2 \mathrm{Zr}(1)$ | $2 \cdot 904 \pm 5$ | 2.97 | $-0.07$ |
|  | 4 Co | $2 \cdot 448 \pm 5$ | $2 \cdot 63$ | $-0.18$ |
|  | $2 \mathrm{Ge}(1)$ | $3.078 \pm 7$ | 2.74 | $+0.34$ |
| $\begin{aligned} & \mathrm{Ge}(2) \\ & \mathrm{C} . \mathrm{N} .12 \end{aligned}$ | $2 \mathrm{Zr}(1)$ | $2 \cdot 732 \pm 3$ | 2.97 | -0.24 |
|  | $2 \mathrm{Zr}(2)$ | $2.904 \pm 3$ | 2.97 | $-0.07$ |
|  | 4 Co | $2 \cdot 486 \pm 3$ | 2.63 | $-0.14$ |
|  | ${ }_{2} \mathrm{Ge}(3)$ | $3 \cdot 017 \pm 4$ | 2.74 | $+0.23$ |
|  | $2 \mathrm{Ge}(3)$ | $3 \cdot 026 \pm 3$ | 2.74 | +0.23 |
| $\mathrm{Ge}(3)$ <br> C.N. 14 | $1 \mathrm{Zr}(2)$ | $2.787 \pm 5$ | 2.97 | -0.18 |
|  | 4 Co | $2 \cdot 466 \pm 4$ | 2.63 | $-0 \cdot 16$ |
|  | $2 \mathrm{Ge}(2)$ | $3.017 \pm 4$ | 2.74 | $+0.28$ |
|  | $2 \mathrm{Ge}(2)$ | $3.026 \pm 3$ | 2.74 | +0.29 |
|  | $4 \mathrm{Ge}(3)$ | $3 \cdot 141 \pm 3$ | 2.74 | $+0.40$ |
|  | $1 \mathrm{Ge}(3)$ | $2 \cdot 463 \pm 7$ | 2.45* | $+0.01$ |
| Ge(4) <br> C.N. 10 | $4 \mathrm{Zr}(2)$ | $2 \cdot 906 \pm 11$ | 2.97 | $-0.06$ |
|  | $4 \mathrm{Zr}(1)$ | $2 \cdot 910 \pm 12$ | $2 \cdot 97$ | -0.06 |
|  | $2 \mathrm{Ge}(4)$ | $2 \cdot 615 \pm 43$ | 2.74 | $-0 \cdot 12$ |

Parthé, E., Lux, B. \& Nowotny, H. (1955). Mh. Chem. 86, 859.
Parthé, E. \& Norton, J. T. (1958). Acta Cryst. 11, 14.

Parthé, E., Nowotny, H. \& Schmid, H. (1955). Mh. Chem. 86, 385.
Rossteutscher, W. \& Schubert, K. (1965). Z. Metallk. 56, 813.
Schubert, K. (1964). Kristallstrukturen zweikomponentiger Phasen. Berlin, Göttingen, Heidelberg: Springer-Verlag.
Shoemaker, D. P., Barieau, R. E., Donohue, J. \& Lu, Chia-Si. (1953). Acta Cryst. 6, 241.
Shomaker, C. B. \& Shoemaker, D. P. (1965). Acta Cryst. 18, 37.

Shoemaker, C. B. \& Shoemaker, D. P. (1968a). To be published.
Shoemaker, D. P. \& Shoemaker, C. B. (1968b). In Structural Chemistry and Molecular Biology. San Francisco: Freeman.
Sly, W. G., Shoemaker, D. P. \& van den Hende, J. H. (1962). A Crystallographic Fourier Summation Program, ERFR 3.
Tharp, A. G., Searcy, A. W. \& Nowotny, H. (1958). J. Electrochem. Soc. 105, 473.
Wernick, J. H. (1967). In Intermetallic Compounds. J. H. Westbrook, ed., New York: Wiley.
Westbrook, J. H., DiCerbo, R. K. \& Peat, A. J. (1958). General Electric Company. GE-58 RL 2117.
Wilson, A. J. C. (1942). Nature, Lond. 150, 151.

# The Crystal Structure of 3,5-Dinitro-4-methylbenzoic Acid 

By D.F.Grant<br>Department of Physics, University of St. Andrews, Scotland

and J.P. G. Richards
Viriamu Jones Laboratory, Department of Physics, University College, Cardiff, Wales
(Received 25 March 1968)


#### Abstract

3,5-Dinitro-4-methylbenzoic acid, $\mathrm{C}_{6} \mathrm{H}_{2} . \mathrm{CH}_{3} .\left(\mathrm{NO}_{2}\right)_{2} . \mathrm{COOH}$, crystallizes in space group $P 2_{1} / a$ with four molecules per unit cell. The structure comprises hydrogen-bonded dimers with the nitro groups twisted out of the ring plane by $47.5^{\circ}$ and $38.9^{\circ}$ respectively.


## 1. Introduction

3,5-Dinitro-4-methylbenzoic acid (Fig.1) was synthesized during studies of Friedel-Crafts reactions by Leyshon (1952), who gives details of its preparation, but earlier references to this substance are given by Claus \& Joachim (1891) and Wheeler \& Harris (1927). It was selected for crystallographic study in 1954, the interest at that time being in the extent of the rotation of the nitro-groups out of the plane of the benzene ring, because of the methyl group between them, and also in the hydrogen bonding. Furthermore, the rather high density ( $1.62 \mathrm{~g} . \mathrm{cm}^{-3}$ ) indicated that the structure might well show interesting short non-bonded intermolecular distances.

Various early attempts at solving the structure were unsuccessful, including applications of the sign-determining procedure of Grant, Howells \& Rogers (1957) which was then being developed. Later three-dimensional sign-determining approaches (Grant, Hine \& Richards, 1960) also appeared to fail, and the structure has now been solved using the $I(\theta, \varphi)$ function of Tollin \& Cochran (1964). In retrospect, a refined version of the three-dimensional sign-fixing method did produce a correct set of signs, but these were not recognized
as such at the time. It is intended to publish details of the sign-determining work later; the object of the present paper is to describe the structure and its solution.


Fig. 1. The molecule of 3,5 -dinitro-4-methylbenzoic acid showing the numbering scheme.


[^0]:    * The term 'close packed' should be understood from a purely geometrical point of view, where atoms are considered as rigid spheres. The average atomic volume of intermetallic compounds in an alloy system is generally a smooth funtion of the composition, independent of the structure (for references see Schubert, 1964).

