

Fig. 3. Ball-and-stick drawings of the coordination polyhedra for (a) Ga(1), (b) Ga(2), and (c) Mg. The site symmetries for these atoms are $4mm$, m and mm , respectively. In all cases, the c axis is vertical. Numerals indicate the type of Ga atoms. The central atom is stippled.

Just as gallium possesses a unique structure among the elements, it appears that Ga_5Mg_2 may also have a unique structure. A search of standard references such

as Pearson's (1967) book reveals no A_5B_2 compounds isotypic with Ga_5Mg_2 . Nor does Mg, in fact, form an A_5Mg_2 phase with any of the other Group IIIA elements.

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The Crystal Structure of $Zr_4Co_4Ge_7$ (V-Phase)

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The crystal structure of the V-phase $Zr_4Co_4Ge_7$ has been determined by single-crystal X-ray diffraction analysis. The structure is of a new type with four formula units in a tetragonal unit cell of space group $I4/mmm$ (D_{4h}^{17}), having the dimensions $a = 13.228 \pm 0.004$, $c = 5.229 \pm 0.003$ Å and $c/a = 0.3952 \pm 0.0002$. The structure was refined by the least-squares method, giving a final R value of 0.092 for the 392 independent structure factors observed. It may be characterized as intermediate between the tetrahedrally close packed structures (σ -phase related structures, Laves phases) and the structures of the $CuAl_2$ -type family.

Introduction

In their study of the ternary system titanium–nickel–silicon, Westbrook, DiCerbo & Peat (1958) reported the occurrence of a ternary phase of the composition $Ti_4Ni_4Si_7$ to which they ascribed the name 'V-phase'. Subsequently Jordan (1963) found thirteen isotypic compounds in which the large titanium atoms were replaced by zirconium, niobium or tantalum, the smaller transition metal component nickel by cobalt and iron, and germanium could substitute silicon. The phases were

reported to be nearly homogeneous at the composition 4:4:7, with the possible exemption of two phases, where the exact composition has not been determined. While investigating similar ternary systems (including hafnium as the larger transition metal component) Markiv, Gladyševskij & Fedoruk (1966), Markiv, Gladyševskij, Kripjakevič & Fedoruk (1966) and Markiv (1966) independently discovered a number of isotypic phases at the approximate composition 1:1:2, having a body-centered tetragonal unit cell. This unit cell could be used to index the powder patterns of the V-

phases and it appears therefore that the compounds found by the Ukraine-Russian authors are isotypic with the V-phases. This conclusion is also supported by the similar lists of representatives given by Jordan (1963) and Markiv (1966) (Table 1.) The present investigation was undertaken to establish the crystal structure of these phases.

Table 1. V-phases found by Jordan (1963), +, and Markiv (1966),*

	Silicides			Germanides		
	Fe	Co	Ni	Fe	Co	Ni
Ti		+	+			+
Zr	+	+		+	+	
Hf		*	*		*	
Nb	+	+	+			
Ta	+	+				

Experimental

Specimens and powder patterns of the V-phases were made available to the author through the kindness of Professor P. A. Beck and Mr A. G. Jordan of this laboratory. From the pronounced graininess of the powder photograph of $Zr_4Co_4Ge_7$ it could be concluded that the sample had large grains and therefore was favorable for the isolation of single crystals. The sample which had been prepared from the components of purity greater than 99.9 wt.%, and annealed at 1100°C for four days, was found upon metallographic examination to contain ~3% of a second phase. The presence of the second phase was probably caused by a 0.5% weight loss of mainly germanium (the most volatile component) during the arc melting, thus shifting the overall composition of the sample slightly towards a higher transition metal content. This explains also the somewhat higher experimental density of $8.13 \pm 0.08 \text{ g.cm}^{-3}$ versus the value of 8.05 g.cm^{-3} deduced from the structure determination.

Several single crystals, isolated from the crushed sample, were examined with a Buerger precession camera (Mo $K\alpha$ radiation) and a Weissenberg goniometer (Cr $K\alpha$ and Mo $K\alpha$ radiation). The body-centered tetragonal unit cell as reported by Markiv (1966) ($a = 13.20$, $c = 5.23 \text{ \AA}$) was confirmed and the following lattice constants were obtained by the least-squares refinement of data taken with a 114.6 mm diameter Debye-Scherrer camera and Cr $K\alpha$ radiation ($\lambda_{K\alpha 1} = 2.28962 \text{ \AA}$):

$$a = 13.228 \pm 0.004, \quad c = 5.229 \pm 0.003 \text{ \AA}$$

$$c/a = 0.3953 \pm 0.0002, \quad V = 915.0 \pm 1.1 \text{ \AA}^3.$$

To facilitate the identification of V-phases, the observed and calculated intensities (using the positional parameters from the refined structure and a computer program by Jeitschko & Parthé, 1966) for a Debye-Scherrer diagram are listed in Table 2.

For the structure determination and refinement, intensity data were collected with a Weissenberg camera, with Mo $K\alpha$ radiation and the multiple film technique (five films interleaved with Cu foils). Intensities were estimated visually with the aid of an intensity strip, which was logarithmically scaled in steps of 10%. The reciprocal lattice planes ($hk0$), ($hk1$), ($hk2$), (hhl) and ($h, h-1, l$) were evaluated. The two single crystals selected for these photographs were both of elongated prismatic shape with rectangular cross-sections and

Table 2. Calculated and observed intensities of the V-phase $Zr_4Co_4Ge_7$

Debye-Scherrer camera, Cr $K\alpha$ radiation.

h	k	l	d_c (Å)	I_c	I_o	h	k	l	d_c (Å)	I_c	I_o
1	1	0	9.3536	2	-	8	4	0	1.4789	4	vw
2	0	0	6.6140	1	-	9	1	0	1.4608	0	-
1	0	1	4.8628	0	-	5	0	3	1.4555	14	s
2	2	0	4.6768	0	-	4	3	3	1.4555	14	s
3	1	0	4.1831	0	-	7	3	2	1.4468	9	w
2	1	1	3.9179	0	-	5	2	3	1.4215	1	-
3	0	1	3.3709	0	-	9	0	1	1.4149	2	vw
4	0	1	3.3070	0	-	8	0	2	1.3975	0	-
3	3	0	3.1179	1	-	9	3	0	1.3944	2	vw
3	2	1	3.0033	1	-	9	2	1	1.3836	0	-
4	2	0	2.9579	0	-	7	6	1	1.3836	5	vw
4	1	1	2.7346	1	-	8	2	2	1.3673	5	vw
0	0	2	2.6145	14	w	6	1	3	1.3601	1	-
5	1	0	2.5942	4	vw	8	5	1	1.3543	2	vw
1	1	2	2.5180	0	-	6	6	2	1.3390	2	vw
2	0	2	2.4314	0	-	7	7	0	1.3362	2	vw
4	3	1	2.3607	51	vs	5	4	3	1.3322	3	vw
5	0	1	2.3607	49	vs	7	5	2	1.3255	2	vw
4	4	0	2.3384	17	w	8	6	0	1.3228	0	-
2	2	2	2.2821	6	vw	10	0	0	1.3228	2	vw
5	3	0	2.2686	1	-	0	0	4	1.3072	16	m
5	2	1	2.2233	4	vs	6	3	3	1.3060	1	-
3	1	2	2.2171	46	vs	9	4	1	1.3009	0	-
6	0	0	2.2047	23	m	10	2	0	1.2971	1	-
6	2	0	2.0915	2	vw	1	1	4	1.2947	0	-
4	0	2	2.0510	8	vw	8	4	2	1.2873	9	w
6	1	1	2.0079	2	w	9	5	0	1.2848	2	w
3	3	2	2.0034	11	w	2	0	4	1.2824	0	-
4	2	2	1.9589	13	w	7	0	3	1.2812	6	vw
5	4	1	1.9214	5	vw	10	1	1	1.2764	5	w
7	1	0	1.8707	0	w	9	1	2	1.2752	7	w
5	5	0	1.8707	7	w	2	2	4	1.2590	0	-
6	3	1	1.8451	1	-	7	2	3	1.2578	1	-
5	1	2	1.8415	0	-	3	1	4	1.2477	0	-
6	4	0	1.8344	3	vw	10	3	1	1.2314	8	w
7	0	1	1.7772	7	w	9	3	2	1.2303	2	w
4	4	2	1.7430	0	-	10	4	0	1.2282	32	s
7	3	0	1.7369	5	vw	4	0	4	1.2157	0	-
1	0	3	1.7281	0	-	6	5	3	1.2147	9	w
7	2	1	1.7163	1	-	8	7	1	1.2106	6	vw
5	3	2	1.7135	0	-	3	3	4	1.2056	0	-
6	0	2	1.6854	0	-	11	1	0	1.1976	0	-
2	1	3	1.6719	0	-	4	2	4	1.1957	0	-
8	0	0	1.6535	3	vw	7	4	3	1.1947	1	vw
6	2	2	1.6332	4	vw	8	1	3	1.1947	5	vw
3	0	3	1.6209	0	-	9	6	1	1.1908	0	-
6	5	1	1.6113	7	w	7	7	2	1.1898	27	s
8	2	0	1.6041	1	-	8	6	2	1.1803	11	vs
3	2	3	1.5744	0	-	10	0	2	1.1803	37	vs
8	1	1	1.5655	3	vw	11	0	1	1.1720	5	vw
7	4	1	1.5655	0	-	8	8	0	1.1692	0	-
6	6	0	1.5589	1	-	5	1	4	1.1674	4	vw
7	5	0	1.5377	0	-	10	2	2	1.1620	4	vw
4	1	3	1.5316	0	-	9	7	0	1.1602	1	-
5	5	2	1.5214	4	w	11	3	0	1.1602	1	-
7	1	2	1.5214	2	w	8	3	3	1.1575	0	-
6	4	2	1.5016	0	-	10	5	1	1.1540	66	vs
8	3	1	1.4845	0	-	11	2	1	1.1540	0	-

both were mounted with the needle axis perpendicular to the primary X-ray beam. The one, rotating around the [001] axis, had the dimensions $0.03 \times 0.05 \times 0.20$ mm the other, with dimensions $0.03 \times 0.03 \times 0.15$ mm, was rotating around the [110] direction. Absorption corrections were made, assuming cylindrical shapes for the crystals (*International Tables for X-ray Crystallography*, 1959). After applying the proper Lorentz-polarization corrections, the structure factors were brought to a common scale by deriving average scale factors using those data present on corresponding films.

Derivation of the approximate structure

From the value of the experimental density mentioned above, the number of formula units per cell was calculated to be $4.04 \approx 4$. The only systematic extinctions observed were those of the body-centered unit cell, and, since the values of $|F(hkl)|$ and $|F(\bar{h}kl)|$ were equal within the limits of error, the structure is of high Laue symmetry, thus reducing the choice to five possible space groups with the general diffraction symbol $I4/**$ (Donnay & Kennard, 1964).

It was noticed that the reciprocal lattice layers with $\Delta l = \pm 4$ were equal except for the normal decline with higher l -values. The quantitative evaluation of the two Weissenberg photographs (h, h, l) and $(h, h-1, l)$ showed that this relation held up to $l=12$, which was the limit of the Mo $K\alpha$ -sphere. Thus the structure is layered with atoms arranged in planes which are $\Delta z = \frac{1}{4}$ apart. This made it possible to compute three-dimensional Patterson functions with the data $(hk0)$, $(hk1)$ and $(hk2)$ only. In order to do this, unitary structure factors were calculated by dividing the observed structure factors by the average atomic scattering coefficient and the average temperature factor, which was obtained from a Wilson plot (Wilson, 1942). The unitary structure factors of the reciprocal planes $l > 2$ were then set equal to the corresponding planes $l \leq 2$. The evaluation of the three-dimensional sharpened Patterson function calculated with these data, using a computer program by Sly, Shoemaker & van den Hende (1962), turned out to be difficult, since even on

the basis of the Patterson function no unambiguous decision could be made among the five possible space groups. Since, however, the z -projection symmetry for the five space groups is the same, it was attempted to gain as much information as possible from the $(hk0)$ data first.

A number of considerations were helpful for the tentative placement of atoms in the z axis projection:

(a) The unitary structure factor U_{1010} has a value very close to unity. Thus one can draw a sublattice which offers 21 possible locations for the placement of the $3\frac{1}{2}$ atoms within the asymmetric unit.

(b) Because of the pseudo-octagonality of the $(hk0)$ reciprocal lattice net (Fig. 1) the arrangement of atoms around the [100] and [110] axes has to be similar in the z -projection.

(c) The length of the z axis makes a placement of two zirconium atoms above each other extremely unlikely.

(d) Additional information was obtained from an electron-density projection computed with about 15 structure factors, for which the signs had been determined with the aid of Harker-Kasper inequalities (Harker & Kasper, 1948).

The combined results of these considerations provided several positions which were likely to be occupied. These positions were then tried out systematically – by assuming distinct z parameters – as starting positions for the interpretation of the three-dimensional Patterson function with the superposition method (a detailed description of this method is given by Shoemaker, Barieau, Donohue & Lu, 1953). After several trials a self-consistent set of atomic positions was obtained. The distribution of the three kinds of atoms was then concluded from the interatomic distances, the weights of the Patterson peaks and from the atomic arrangements in related compounds. An intensity calculation with this trial structure gave an R value (defined throughout the paper as $R = \Sigma |F_o - F_c| / \Sigma F_o$) of 0.18 for the observed structure factors, indicating that the structure was essentially correct.

Structure refinement

The structure was refined on the University of Illinois IBM 7094 computer with a full-matrix least-squares program (Gantzel, Sparks & Trueblood, 1961) and the function minimized was $\Sigma w^2(\Delta F)^2$ with $w = 1/F_{\text{obs}}$. Although the structure may be described with all five space groups of $I4/**$, the space group with the highest symmetry: $I4/mmm - D_{4h}^{17}$ was chosen for the refinement. This is the most probable space group, since the description of the structure in space groups $I\bar{4}2m$, $I4m2$ and $I4mm$ would allow, besides an increase in the number of x and y parameters, three or six additional z parameters, which are not required because of the layered nature of the structure, as mentioned above. The fifth possible space group, $I422$, was not ruled out initially, since it requires only one additional parameter: the 16 cobalt atoms of position $16(k)$ in $I4/mmm$

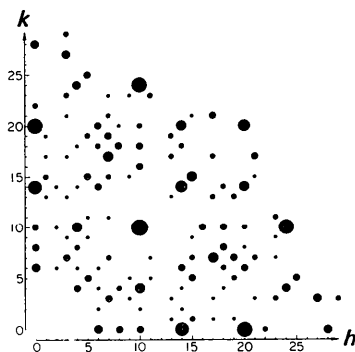


Fig. 1. Unitary structure factors in the reciprocal lattice plane $(hk0)$ of $Zr_4Co_4Ge_7$, showing pseudo-octagonal symmetry.

Discussion

The V-phase structure (Fig. 2) may be described as intermediate between two structure families: the tetrahedrally close packed structures and the CuAl_2 -type family. The tetrahedrally close packed structures are characterized by the predominance of fairly regular coordination polyhedra of coordination numbers (C.N.) 12, 14, 15 and 16 (Frank & Kasper, 1958, 1959). Shoemaker & Shoemaker (1968*a*) have proposed the name 'tetrahedrally close packed structures' for these phases, since they have slightly distorted tetrahedral voids only. They have typically metallic character, *i.e.* their occurrence and varying compositions are governed by valence electron rules (Greenfield & Beck, 1956; Das & Beck, 1960; Bardos & Beck, 1966; Laves & Witte, 1936; Klee & Witte 1954; Nevitt, 1963; Wernick, 1967). This group of compounds may be divided into two subgroups. The one, commonly called the σ -phase related structures (for references see Shoemaker & Shoemaker, 1968*a, b*) is formed by metals of not more than 15% difference in atomic radii (C.N. 12). The structures of the other subgroup, the Laves phases (MgNi_2 -type, MgCu_2 -type and MgZn_2 -type, for references see Nevitt, 1963) are formed by elements differing about 10 to 60% in atomic radii. These

structures are distinguished from the σ -phase related structures in so far as they have C.N. 12 and C.N. 16 polyhedra only. The lack of intermediate coordination polyhedra is probably responsible for the occurrence of the Laves phases in ternary systems along the pseudo-binary sections $A(B,C)_2$ only, in contrast to the σ -phase related structures where the C.N. 14 and C.N. 15 sites can accommodate both small and large atoms (Shoemaker & Shoemaker, 1965).

The CuAl_2 family comprises a number of structures (CuAl_2 -type, U_3Si_2 -type, C_5B_3 -type structures) which may be described as stacking variants of the tessellation net 3².4.3.4, formed by the larger atoms only (Aronsson, 1961). The structure types W_5Si_3 , Mn_5Si_3 and Ti_5Ga_4 (for references see Schubert, 1964) with a transition metal/meta metal ratio similar to that of the V-phase may be regarded, like the V-phase structure, as intermediate between the tetrahedrally close packed structures and the structures of the CuAl_2 family (Aronsson, 1961). The structural relationships among these various silicide structure types have been discussed by Parthé, Lux & Nowotny (1955) and Nowotny (1963).

Like most of the tetrahedrally close packed structures and the structures of the CuAl_2 family, the V-phase is a layered structure. It has two identical main layers at $z=0$ and $\frac{1}{2}$, translated, relative to each other

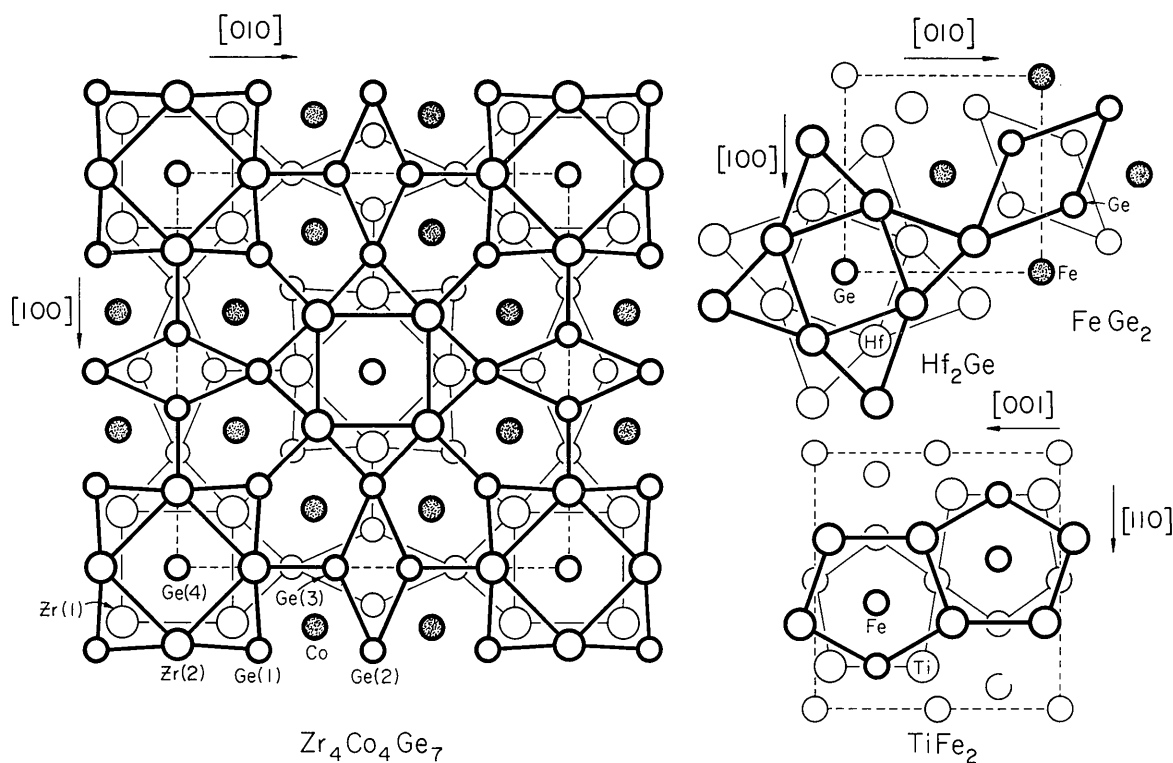


Fig. 2. Structure of the V-phase $\text{Zr}_4\text{Co}_4\text{Ge}_7$ as compared to the structures of Hf_2Ge and FeGe_2 (both crystallizing in the CuAl_2 -type) and TiFe_2 (MgZn_2 -type). The outlined building elements in the CuAl_2 and MgZn_2 -type structures are very similar to those present in $\text{Zr}_4\text{Co}_4\text{Ge}_7$. In the drawing of the $\text{Zr}_4\text{Co}_4\text{Ge}_7$ structure the atoms at $z = \frac{1}{2}$ are connected with thick lines, atoms at $z = 0$ with thin lines and non connected atoms are superimposed with $z = \frac{1}{4}$ and $\frac{3}{4}$.

by half the base diagonal. These layers are formed by the Zr atoms and the Ge atoms (1), (2) and (3) which are in contact with each other, thus forming a tessellation of pentagons, squares and triangles (Fig. 2). The Co and Ge(4) atoms are situated at $z = \frac{1}{4}$ and $\frac{3}{4}$ and have no close neighbors within their layers. The structure exhibits a high degree of close packing.* However it should not be considered as a purely tetrahedrally close packed structure since some of the tetrahedra have edges differing by more than 40% in length; furthermore it does not contain Frank-Kasper polyhedra only. It is interesting to note that the tetrahedrally close packed structures and the structures of the $CuAl_2$ family occur most frequently in the binary systems of the components forming a V-phase. The structural relationship of the V-phase to these structure types can be demonstrated by comparison of the coordination polyhedra.

As can be seen from Fig. 3 the environments of the Zr atoms (1) and (2) are the same, if one disregards some minor differences in the interatomic distances (Table 5). This coordination polyhedron may be derived from the Frank-Kasper polyhedron C.N. 15 by replacing each of two atoms from the 'belt' by a pair of atoms at the same level, whereby the C.N. is increased to 17. A similar arrangement is also found around the Hf^I atom in $Hf_3^I Hf_2^II Sn_4$ (Ti_5Ga_4 -type, Rossteutscher & Schubert, 1965) where the places of Zr are taken by Hf^I , those of Co by Hf^II and those of Ge by Sn. The coordination polyhedra for the Co and Ge(2) atoms are distorted icosahedra, which are present in all tetrahedrally close packed structures. The environment of Ge(1) is the same as that of Ge(2) except for the replacement of two neighboring Ge atoms by a Zr atom. This C.N. 11 polyhedron is also found for the Ge atoms in Zr_5Ge_3 (Mn_5Si_3 -type, Parthé & Norton, 1958), where the places of both transition metals Zr and Co are occupied by Zr. The coordination around Ge(3) is the Frank-Kasper polyhedron C.N. 14. However, the distance of 2.46 Å to one of the crystallographically equivalent Ge atoms is very close to the covalent bonding distance of 2.45 Å in elemental germanium (diamond-type). Thus the Ge(3) atoms may be considered as forming pairs. The Ge atoms in Th_3Ge_2 (U_3Si_2 -type, Tharp, Searcy & Nowotny, 1958) and $FeGe_2$ ($CuAl_2$ -type, Krén & Szabó, 1964) have similar environments with short Ge-Ge distances of 2.4₈ and 2.62 respectively. The Ge(4) atoms are situated in a tetragonal antiprism of Zr atoms with two Ge atoms above and below the square faces. This C.N. 10 polyhedron is also found for the Ge atoms in Hf_2Ge ($CuAl_2$ -type, Nowotny, Benesovsky & Schob, 1960) and the Si atoms of the fourfold positions in Nb_5Si_3

and Ta_5Si_3 (W_5Si_3 -type, Parthé, Nowotny & Schmid, 1955).

In Table 5 the interatomic distances in $Zr_4Co_4Ge_7$ are compared with the sum of the atomic radii for C.N. 12. There is a strong interaction of the transition metals with germanium (all distances Zr-Ge and Co-Ge are shorter than the corresponding sums of the C.N. 12 radii). The distances Zr-Zr, Zr-Co and Co-Co are all longer. The only short Ge-Ge distances are found for Ge(4), forming chains and Ge(3) forming pairs as already mentioned above.

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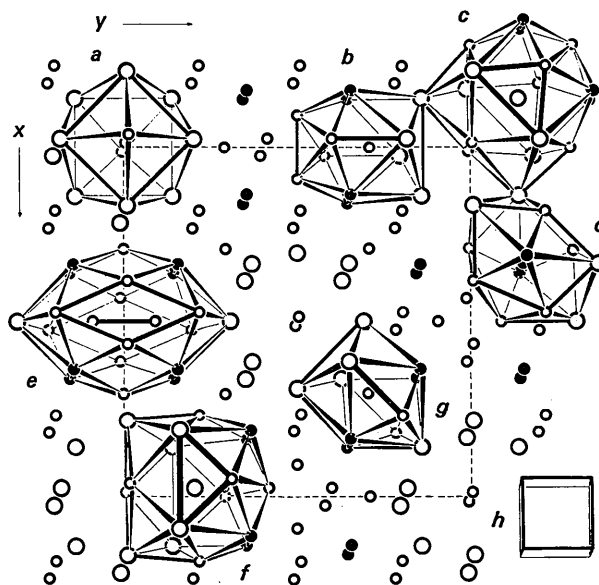


Fig. 3. Coordination polyhedra in $Zr_4Co_4Ge_7$. Co atoms are represented by black spheres, Zr and Ge atoms by large and small white spheres respectively. The environment of Zr (1) and Zr (2) is shown in c and f; a, b and g are the coordination polyhedra of Ge(4), Ge(2) and Ge(1) respectively; d shows the distorted icosahedron around the Co atoms and e is the coordination polyhedron around a pair of Ge(3) atoms. A cube with the cube edge $a = c/2$ as seen from the same viewpoint is drawn in h.

* The term 'close packed' should be understood from a purely geometrical point of view, where atoms are considered as rigid spheres. The average atomic volume of intermetallic compounds in an alloy system is generally a smooth function of the composition, independent of the structure (for references see Schubert, 1964).

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Table 5. Interatomic distances D and coordination numbers $C.N.$ in the structure of $Zr_4Co_4Ge_7$ For comparison the sum of the atomic radii ($CN\ 12$) is listed too. All distances shorter than $3.8\ \text{\AA}$ are given.

		$D\ [\text{\AA}]$	$r_A + r_B\ [\text{\AA}]$	$\Delta\ [\text{\AA}]$
Zr(1) C.N. 17	4 Zr(2)	3.285 ± 3	3.20	+0.09
	2 Zr(1)	3.677 ± 9	3.20	+0.48
	4 Co	3.106 ± 6	2.86	+0.25
	2 Ge(2)	2.732 ± 3	2.97	-0.24
	1 Ge(1)	2.888 ± 9	2.97	-0.08
	2 Ge(1)	2.904 ± 5	2.97	-0.07
	2 Ge(4)	2.910 ± 12	2.97	-0.06
Zr(2) C.N. 17	4 Zr(1)	3.285 ± 3	3.20	+0.09
	2 Zr(2)	3.670 ± 5	3.20	+0.47
	4 Co	3.129 ± 3	2.86	+0.27
	2 Ge(1)	2.736 ± 6	2.97	-0.23
	1 Ge(3)	2.787 ± 5	2.97	-0.18
	2 Ge(2)	2.904 ± 3	2.97	-0.07
	2 Ge(4)	2.906 ± 11	2.97	-0.06
Co C.N. 12	2 Zr(1)	3.106 ± 6	2.86	+0.25
	2 Zr(2)	3.129 ± 3	2.86	+0.27
	2 Co	2.615 ± 2	2.52	+0.10
	2 Ge(1)	2.448 ± 5	2.63	-0.18
	2 Ge(3)	2.466 ± 4	2.63	-0.16
	2 Ge(2)	2.486 ± 3	2.63	-0.14
Ge(1) C.N. 11	2 Zr(2)	2.736 ± 6	2.97	-0.23
	1 Zr(1)	2.888 ± 9	2.97	-0.08
	2 Zr(1)	2.904 ± 5	2.97	-0.07
	4 Co	2.448 ± 5	2.63	-0.18
	2 Ge(1)	3.078 ± 7	2.74	+0.34
Ge(2) C.N. 12	2 Zr(1)	2.732 ± 3	2.97	-0.24
	2 Zr(2)	2.904 ± 3	2.97	-0.07
	4 Co	2.486 ± 3	2.63	-0.14
	2 Ge(3)	3.017 ± 4	2.74	+0.23
	2 Ge(3)	3.026 ± 3	2.74	+0.29
Ge(3) C.N. 14	1 Zr(2)	2.787 ± 5	2.97	-0.18
	4 Co	2.466 ± 4	2.63	-0.16
	2 Ge(2)	3.017 ± 4	2.74	+0.28
	2 Ge(2)	3.026 ± 3	2.74	+0.29
	4 Ge(3)	3.141 ± 3	2.74	+0.40
	1 Ge(3)	2.463 ± 7	2.45*	+0.01
Ge(4) C.N. 10	4 Zr(2)	2.906 ± 11	2.97	-0.06
	4 Zr(1)	2.910 ± 12	2.97	-0.06
	2 Ge(4)	2.615 ± 43	2.74	-0.12

* Ge-Ge distance in elemental germanium (diamond type).

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The Crystal Structure of 3,5-Dinitro-4-methylbenzoic Acid

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3,5-Dinitro-4-methylbenzoic acid, $C_6H_2 \cdot CH_3 \cdot (NO_2)_2 \cdot COOH$, crystallizes in space group $P2_1/a$ with four molecules per unit cell. The structure comprises hydrogen-bonded dimers with the nitro groups twisted out of the ring plane by 47.5° and 38.9° respectively.

1. Introduction

3,5-Dinitro-4-methylbenzoic acid (Fig. 1) was synthesized during studies of Friedel-Crafts reactions by Leyshon (1952), who gives details of its preparation, but earlier references to this substance are given by Claus & Joachim (1891) and Wheeler & Harris (1927). It was selected for crystallographic study in 1954, the interest at that time being in the extent of the rotation of the nitro-groups out of the plane of the benzene ring, because of the methyl group between them, and also in the hydrogen bonding. Furthermore, the rather high density (1.62 g. cm^{-3}) indicated that the structure might well show interesting short non-bonded intermolecular distances.

Various early attempts at solving the structure were unsuccessful, including applications of the sign-determining procedure of Grant, Howells & Rogers (1957) which was then being developed. Later three-dimensional sign-determining approaches (Grant, Hine & Richards, 1960) also appeared to fail, and the structure has now been solved using the $I(\theta, \varphi)$ function of Tollin & Cochran (1964). In retrospect, a refined version of the three-dimensional sign-fixing method did produce a correct set of signs, but these were not recognized

as such at the time. It is intended to publish details of the sign-determining work later; the object of the present paper is to describe the structure and its solution.

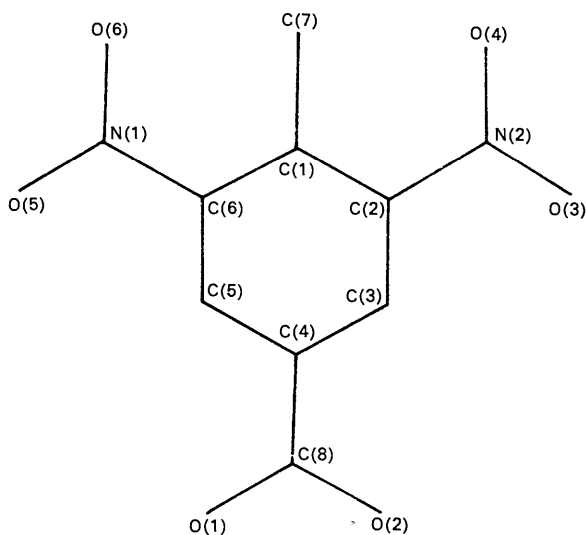


Fig. 1. The molecule of 3,5-dinitro-4-methylbenzoic acid showing the numbering scheme.